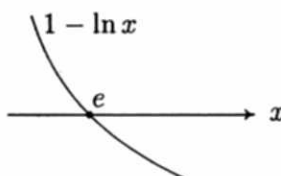
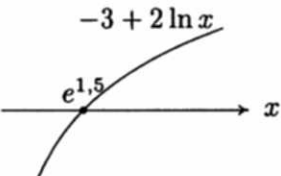


Nr		BE																
1.1	$f(x) = \frac{\ln x}{x}, \quad D_f = \mathbb{R}^+, \quad \text{NSt.: } x = 1$ $x \rightarrow +0 \Rightarrow f(x) = \frac{\ln x}{x} \rightarrow \frac{-\infty}{+0} \rightarrow -\infty; \quad \lim_{\substack{x \rightarrow 0 \\ x > 0}} f(x) = -\infty \Rightarrow x = 0 \text{ vert. A. von } G_f$ $x \rightarrow \infty \Rightarrow f(x) = \frac{\ln x}{x} \rightarrow \frac{+\infty}{+\infty} \text{ l'H. } \rightarrow \frac{\frac{1}{x}}{1} = \frac{1}{x} \rightarrow +0$ $\lim_{x \rightarrow \infty} f(x) = 0 \Rightarrow y = 0 \text{ ist horizontale Asymptote von } G_f$																	
1.2	$f'(x) = \frac{x \cdot \frac{1}{x} - (\ln x) \cdot 1}{x^2} = \frac{1 - \ln x}{x^2}$ $f''(x) = \frac{x^2 \cdot \left(-\frac{1}{x}\right) - (1 - \ln x) \cdot 2x}{x^4} = \frac{-x - 2x(1 - \ln x)}{x^4} = \frac{-3x + 2x \ln x}{x^4} = \frac{-3 + 2 \ln x}{x^3}$																	
1.3	<p>Monotonie: $f'(x) = 0: 1 - \ln x = 0 \Leftrightarrow \ln x = 1 \Leftrightarrow x = e, \quad f(e) = \frac{\ln e}{e} = \frac{1}{e}$</p> <table style="display: inline-table; vertical-align: middle;"> <tr> <td style="padding-right: 10px;">$D_f:$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 10px;">0</td> <td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 10px;">e</td> <td style="border-left: 1px solid black; padding: 0 10px;">x</td> </tr> <tr> <td>$1 - \ln x:$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">-</td> <td></td> </tr> <tr> <td>$x^2:$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td></td> </tr> <tr> <td>$f'(x):$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">-</td> <td></td> </tr> </table> <p style="text-align: center; margin-left: 100px;">HOP</p>  <p>f streng monoton zunehmend in $]0; e]$ und streng monoton abnehmend in $[e; \infty[\Rightarrow H(e \frac{1}{e})$ Hochpunkt</p>	$D_f:$	0	e	x	$1 - \ln x:$	+	-		$x^2:$	+	+		$f'(x):$	+	-		
$D_f:$	0	e	x															
$1 - \ln x:$	+	-																
$x^2:$	+	+																
$f'(x):$	+	-																
1.4	<p>Krümmung: $f''(x) = 0: -3 + 2 \ln x = 0 \Leftrightarrow 2 \ln x = 3 \Leftrightarrow \ln x = \frac{3}{2} = 1,5 \Leftrightarrow x = e^{1,5}$</p> $f(e^{1,5}) = \frac{\ln(e^{1,5})}{e^{1,5}} = \frac{1,5}{e^{1,5}}$ <table style="display: inline-table; vertical-align: middle;"> <tr> <td style="padding-right: 10px;">$D_f:$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 10px;">0</td> <td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 10px;">$e^{1,5}$</td> <td style="border-left: 1px solid black; padding: 0 10px;">x</td> </tr> <tr> <td>$-3 + 2 \ln x:$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">-</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td></td> </tr> <tr> <td>$x^3:$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td></td> </tr> <tr> <td>$f''(x):$</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">-</td> <td style="border-left: 1px solid black; border-right: 1px solid black; text-align: center;">+</td> <td></td> </tr> </table> <p style="text-align: center; margin-left: 100px;">WP</p>  <p>G_f rechtsgekrümmt in $]0; e^{1,5}]$ und linksgekrümmt in $[e^{1,5}; \infty[\Rightarrow W(e^{1,5} \frac{1,5}{e^{1,5}})$ Wendepunkt</p>	$D_f:$	0	$e^{1,5}$	x	$-3 + 2 \ln x:$	-	+		$x^3:$	+	+		$f''(x):$	-	+		
$D_f:$	0	$e^{1,5}$	x															
$-3 + 2 \ln x:$	-	+																
$x^3:$	+	+																
$f''(x):$	-	+																
1.5	